

The quadprog Package

February 16, 2008

Version 1.4-11

Date 2007-07-12

Title Functions to solve Quadratic Programming Problems.

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Description This package contains routines and documentation for solving quadratic programming problems.

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`solve.QP` *Solve a Quadratic Programming Problem*

Description

This routine implements the dual method of Goldfarb and Idnani (1982, 1983) for solving quadratic programming problems of the form $\min(-d^T b + 1/2 b^T D b)$ with the constraints $A^T b \geq b_0$.

Usage

```
solve.QP(Dmat, dvec, Amat, bvec, meq=0, factorized=FALSE)
```

Arguments

Dmat	matrix appearing in the quadratic function to be minimized.
dvec	vector appearing in the quadratic function to be minimized.
Amat	matrix defining the constraints under which we want to minimize the quadratic function.
bvec	vector holding the values of b_0 (defaults to zero).
meq	the first meq constraints are treated as equality constraints, all further as inequality constraints (defaults to 0).
factorized	logical flag: if TRUE, then we are passing R^{-1} (where $D = R^T R$) instead of the matrix D in the argument Dmat.

Value

a list with the following components:

solution	vector containing the solution of the quadratic programming problem.
value	scalar, the value of the quadratic function at the solution
unconstrained.solution	vector containing the unconstrained minimizer of the quadratic function.
iterations	vector of length 2, the first component contains the number of iterations the algorithm needed, the second indicates how often constraints became inactive after becoming active first. vector with the indices of the active constraints at the solution.

References

- Goldfarb, D. and Idnani, A. (1982). Dual and Primal-Dual Methods for Solving Strictly Convex Quadratic Programs. In Numerical Analysis J.P. Hennart, ed. Springer-Verlag, Berlin. pp. 226-239.
- Goldfarb, D. and Idnani, A. (1983). A numerically stable dual method for solving strictly convex quadratic programs. *Mathematical Programming* **27**, 1-33.

See Also

[solve.QP.compact](#)

Examples

```
#
# Assume we want to minimize: -(0 5 0) %*% b + 1/2 b^T b
# under the constraints:      A^T b >= b0
# with b0 = (-8, 2, 0)^T
# and      (-4  2  0)
#      A = (-3  1 -2)
#      ( 0  0  1)
# we can use solve.QP as follows:
#
Dmat      <- matrix(0, 3, 3)
```

```
diag(Dmat) <- 1
dvec    <- c(0, 5, 0)
Amat    <- matrix(c(-4, -3, 0, 2, 1, 0, 0, -2, 1), 3, 3)
bvec    <- c(-8, 2, 0)
solve.QP(Dmat, dvec, Amat, bvec=bvec)
```

solve.QP.compact *Solve a Quadratic Programming Problem*

Description

This routine implements the dual method of Goldfarb and Idnani (1982, 1983) for solving quadratic programming problems of the form $\min(-d^T b + 1/2b^T D b)$ with the constraints $A^T b \geq b_0$.

Usage

```
solve.QP.compact(Dmat, dvec, Amat, Aind, bvec, meq=0, factorized=FALSE)
```

Arguments

Dmat	matrix appearing in the quadratic function to be minimized.
dvec	vector appearing in the quadratic function to be minimized.
Amat	matrix containing the non-zero elements of the matrix A that defines the constraints. If m_i denotes the number of non-zero elements in the i -th column of A then the first m_i entries of the i -th column of $Amat$ hold these non-zero elements. (If $maxmi$ denotes the maximum of all m_i , then each column of $Amat$ may have arbitrary elements from row m_i+1 to row $maxmi$ in the i -th column.)
Aind	matrix of integers. The first element of each column gives the number of non-zero elements in the corresponding column of the matrix A . The following entries in each column contain the indexes of the rows in which these non-zero elements are.
bvec	vector holding the values of b_0 (defaults to zero).
meq	the first <code>meq</code> constraints are treated as equality constraints, all further as inequality constraints (defaults to 0).
factorized	logical flag: if TRUE, then we are passing R^{-1} (where $D = R^T R$) instead of the matrix D in the argument <code>Dmat</code> .

Value

a list with the following components:

solution	vector containing the solution of the quadratic programming problem.
value	scalar, the value of the quadratic function at the solution
unconstrained.solution	vector containing the unconstrained minimizer of the quadratic function.

iterations vector of length 2, the first component contains the number of iterations the algorithm needed, the second indicates how often constraints became inactive after becoming active first. vector with the indices of the active constraints at the solution.

References

Goldfarb, D. and Idnani, A. (1982). Dual and Primal-Dual Methods for Solving Strictly Convex Quadratic Programs. In Numerical Analysis J.P. Hennart, ed. Springer-Verlag, Berlin. pp. 226-239.

Goldfarb, D. and Idnani, A. (1983). A numerically stable dual method for solving strictly convex quadratic programs. Mathematical Programming **27**, 1-33.

See Also

[solve.QP](#)

Examples

```
#
# Assume we want to minimize: -(0 5 0) %*% b + 1/2 b^T b
# under the constraints:      A^T b >= b0
# with b0 = (-8,2,0)^T
# and      (-4 2 0)
#      A = (-3 1 -2)
#           ( 0 0 1)
# we can use solve.QP.compact as follows:
#
Dmat      <- matrix(0,3,3)
diag(Dmat) <- 1
dvec      <- c(0,5,0)
Aind      <- rbind(c(2,2,2),c(1,1,2),c(2,2,3))
Amat      <- rbind(c(-4,2,-2),c(-3,1,1))
bvec      <- c(-8,2,0)
solve.QP.compact(Dmat,dvec,Amat,Aind,bvec=bvec)
```

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